

Engineering-assessed SLR Range biases

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Acknowledgements:

ILRS Signal Processing WG (T Otsubo)

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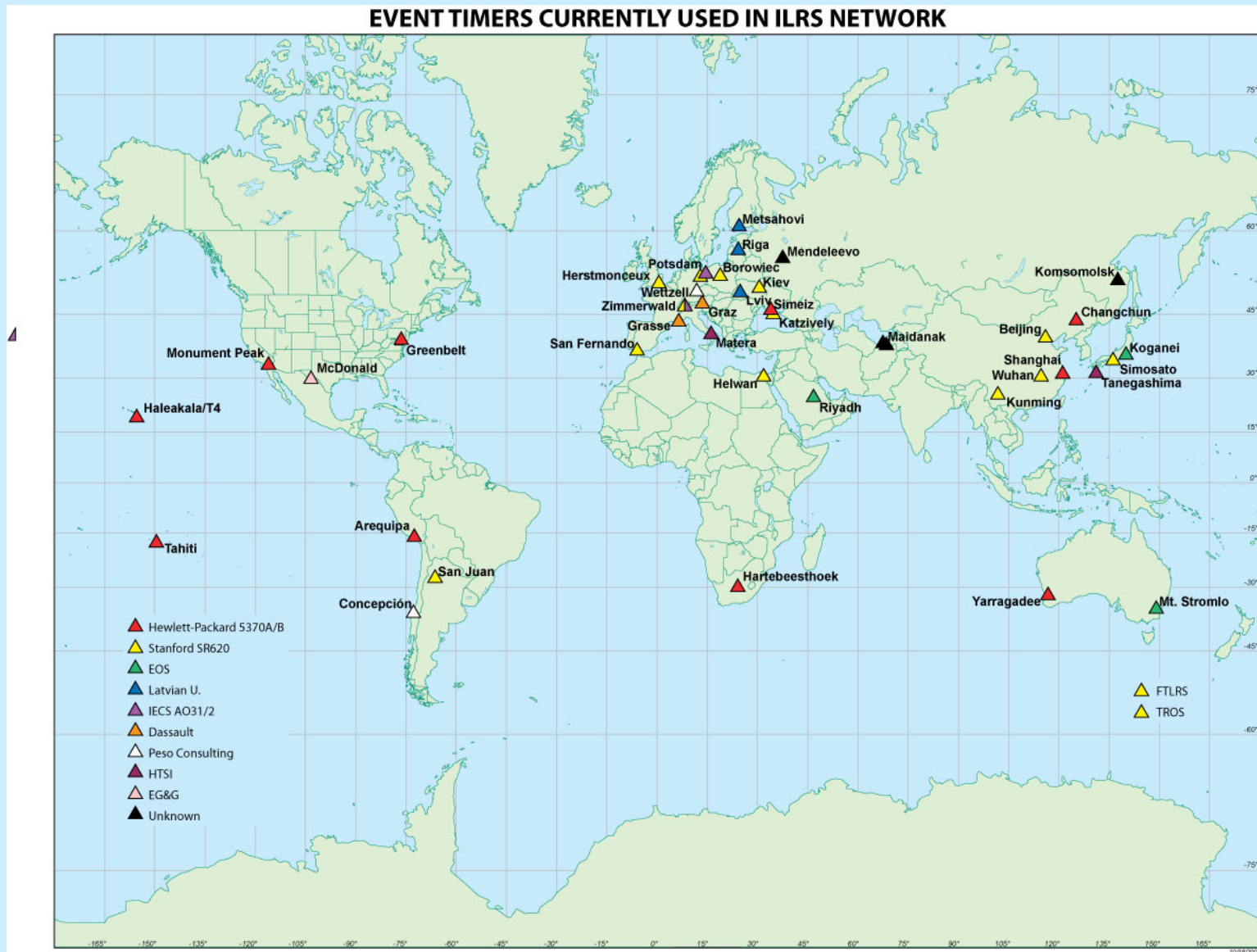
Outline

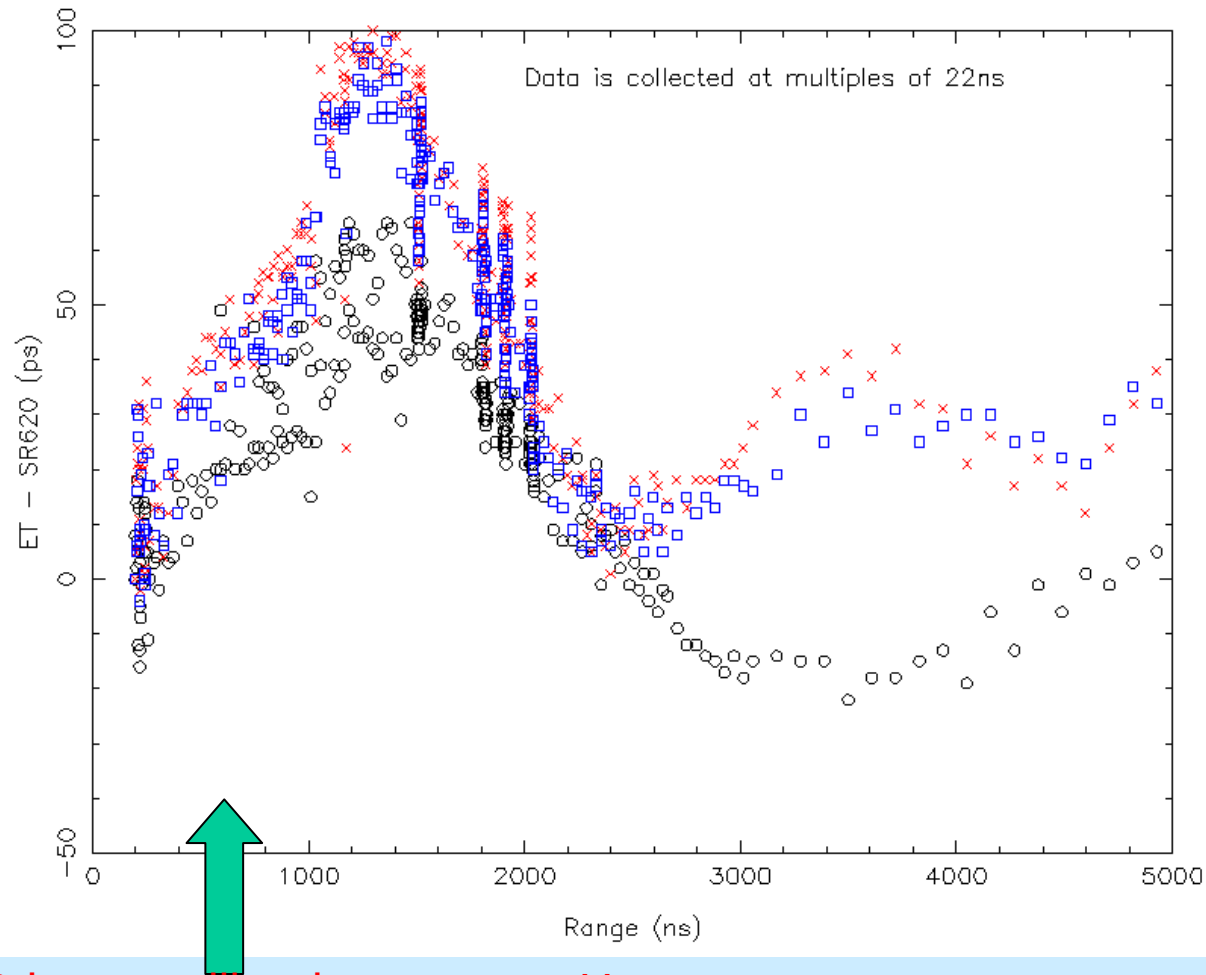
- Laser ranging has a well-known potential for mm-level accuracy which is independent of distance – LEO to Lunar and beyond;
- In the last few years, two issues have emerged that might have threatened this strength for ITRF work:
 - Non-linearity effects in (some) time-of-flight counters;
 - Lack of models for accurate centre of mass corrections for LAGEOS (and ETALON)
- We discuss status of both these issues

Tests on (Stanford) counter linearity

- Relative to a 'perfect' time-of-flight counter, what are the characteristics of the counters in common use over the last 15+ years?
- Work has been carried out on *Stanford* counters in use at Herstmonceux, relative to a high-spec, ps-level event timer.
- Counters from Potsdam and Boroweic also tested at Herstmonceux.
- Studied effects at LAGEOS and at local calibration target distances.

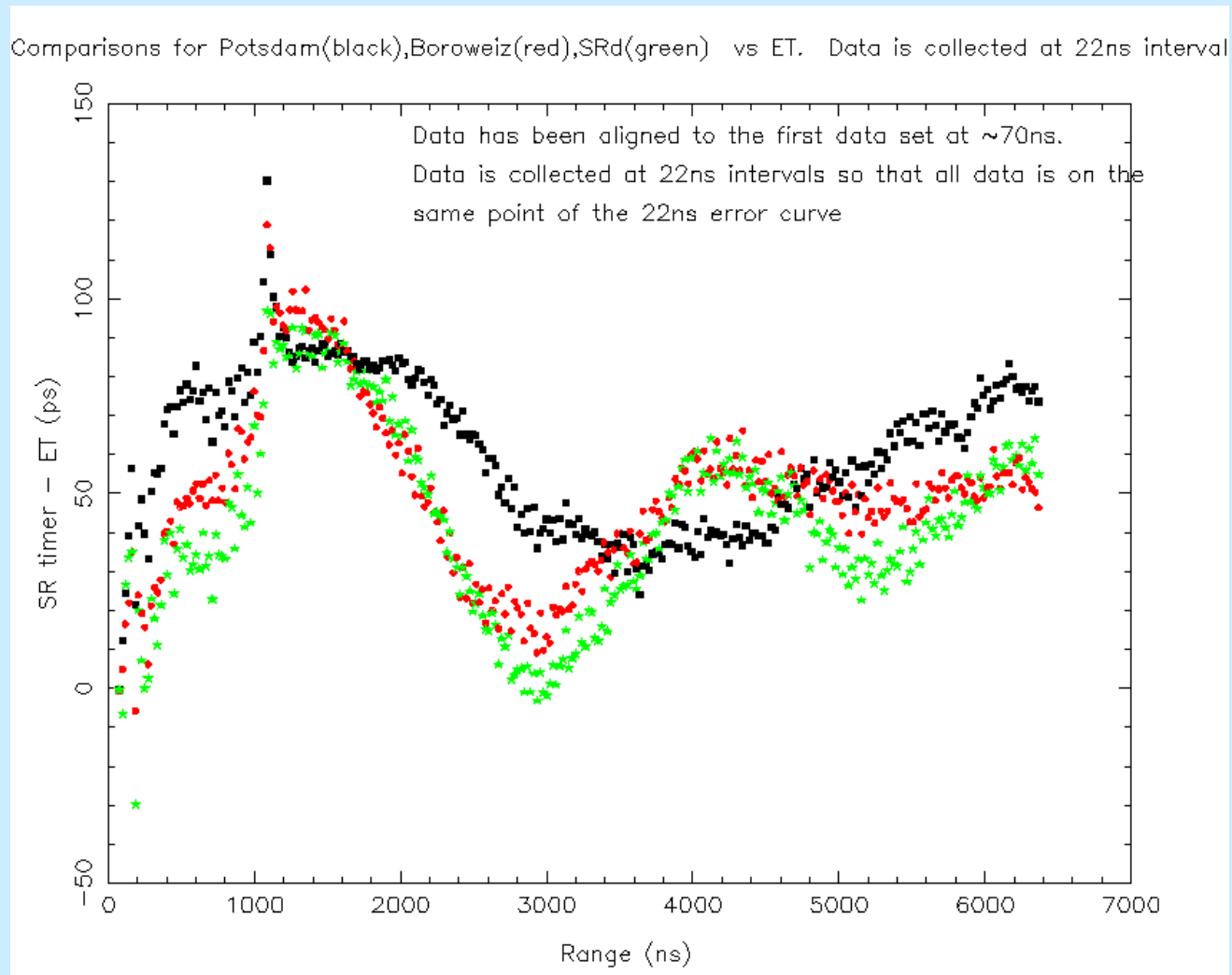
Counters in use in ILRS stations



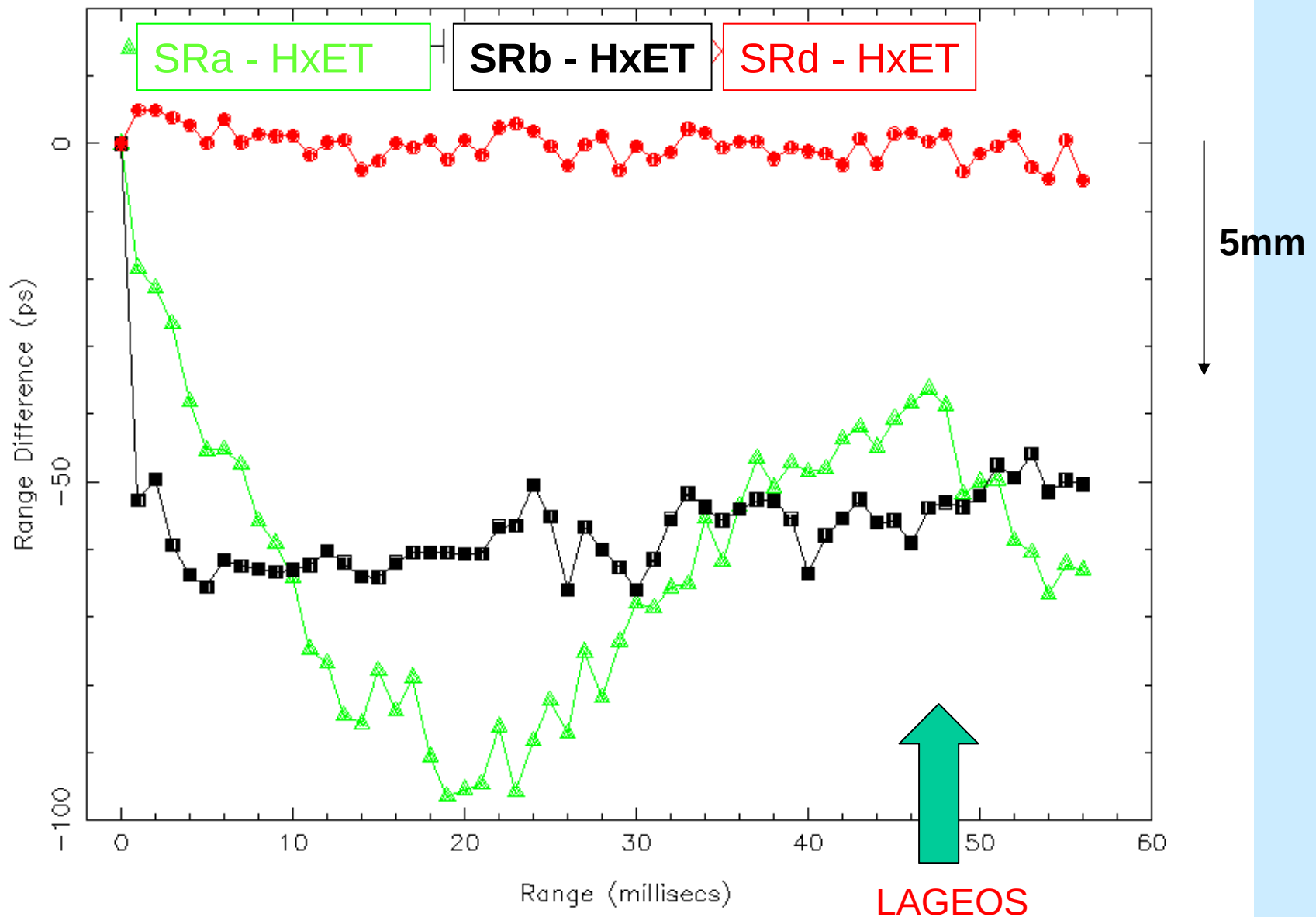


Comparisons between HxET and the Stanford counters for calibration boards' distances;
 Behaviour very similar to spec;
 Errors up to 100ps (15mm), with some systematic detailed structure

Tests at Hx with Potsdam (7836) and Borowiec counters – at calibration ranges



Comparison between Hx ET and SRa,SRb & SRd



Example: effect on range measurements at Herstmonceux (1994-2007)

- The non-linearity of the Stanfords:
- imparts an average of $\sim -5.5 \pm 2\text{mm}$ error onto the observed calibration range;
 - The calibrations are too short;
 - Hence calibrated satellite ranges are too long by 5.5mm.
- Value is dependent on the target range, electronic delays and on the particular Stanford;
 - Hence the inherent 2mm uncertainty in this correction

Example of effect on range measurements at Herstmonceux (1994-2002)

- At distance of LAGEOS, range error is $\sim -8 \pm 2\text{mm}$;
 - observed raw LAGEOS ranges are too short
- So total range error is:
 - $+ 5.5 - 8.0 = - 2.5 \pm 3\text{mm}$
 - i.e. need to add 2.5mm to LAGEOS ranges
- This correction applies to the period 1994 October 1 to 2002 January 31

Summary

Station	Dates	Range Correction (mm)
7840 HERL	1994/10/01 – 2002/01/31	+2.5
7840 HERL	2002/02/01- 2007/02/10	-5.5
7836 POTS	1992/05/01 ->	+3.0
7841 POTS	2001/07/01 – 2004/02/28	+5
7811 BORL	2002/05/01 ->	-9

Estimates for other stations

- Stanford counters;
- Using the methodology outlined above;
- We have made 'worst case' **estimates** of calibration error and total range error at LAGEOS for all 'Stanford stations':
- Error span is -9 to +11mm, frequent error +10mm
- Uncertainty in these **estimates** could be up to ~5mm

Worse-case error estimates (mm)

Station		ID	Calibration error	LAGEOS error	Total error
BEIL	Beijing	7249	-12	+10	- 2
BORL	Borowiec	7811	- 9	+ 0 meas	- 9
BREF	Brest	7604	-10	+10	0
GLSV	Kiev	1824	- 6	+10	+ 4
HELW	Helwan	7831	0	+10	+10
KTZL	Katzively, Ukraine	1893	0	+10	+10
KUNL	Kunming, China	7820	- 9	+10	+ 1
POT3	Potsdam	7841	0	+ 5	+ 5
POTL	Potsdam	7836	0	+ 3 meas	+ 3
SFEL	San Fernando	7824	0	+ 8 meas	+ 8
SISL	Simosato, Japan	7838	+1	+10	+11
SJUL	San Juan	7406	0	+10	+10
WUHL	Wuhan	7231	0	+10	+10
ZIML	Zimmerwald	7810	-3	+ 8 appl	- 3
Closed sites					
GRSL	Grasse	7835	- 1	10	11

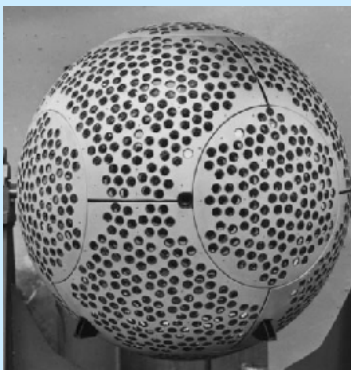
meas = measured on particular Stanford counters; **appl** = applied at station

Comments

- We emphasise the **estimated** nature of this table;
e.g. the 3 Herstmonceux Stanford counters show large inter-counter differences;
- Difficult to test other counters;
 - Either no longer available or still vital to operations
 - Unlikely to make significant further progress
- Several of the stations have already **upgraded** to higher-quality counters.

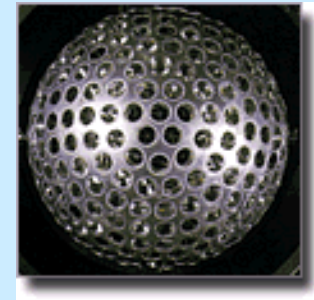
Summary/outlook

- We also note that:
- The stations are a subset of the full ILRS network, but do contain some core sites;
- It is also estimated (Zhong, 1998) that the **HP** counters in common use have non-linearity effects at ~3mm level
 - Needs further investigation

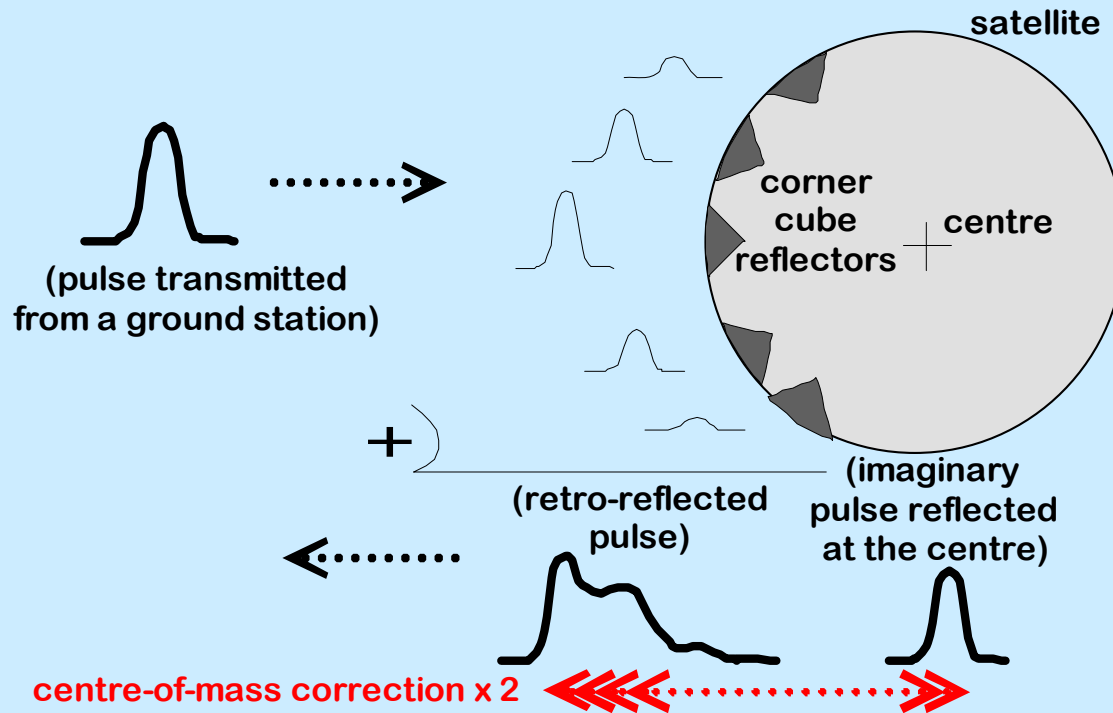


ETALON

Centre of Mass corrections: Satellite 'signature' contribution



LAGEOS

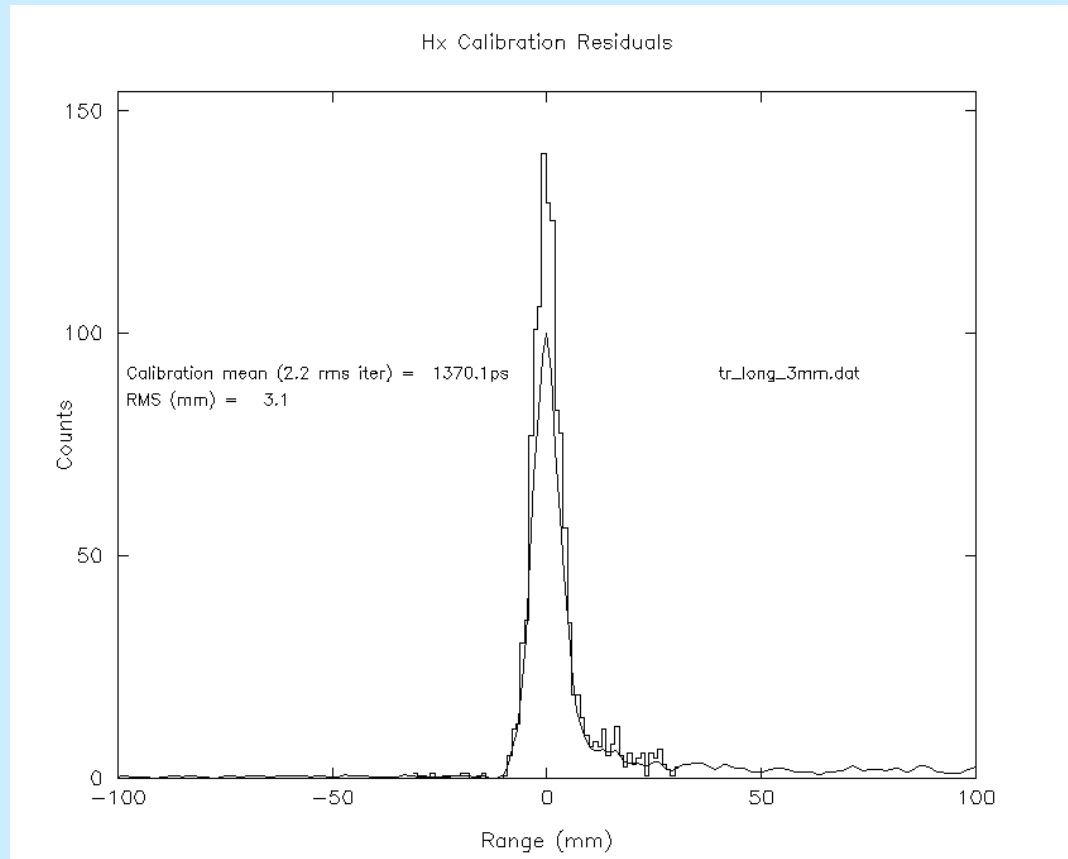


On average, over many shots, returning pulse-shape can be modelled as a convolution of laser pulse-shape with the satellite response function.

Magnitude of effect

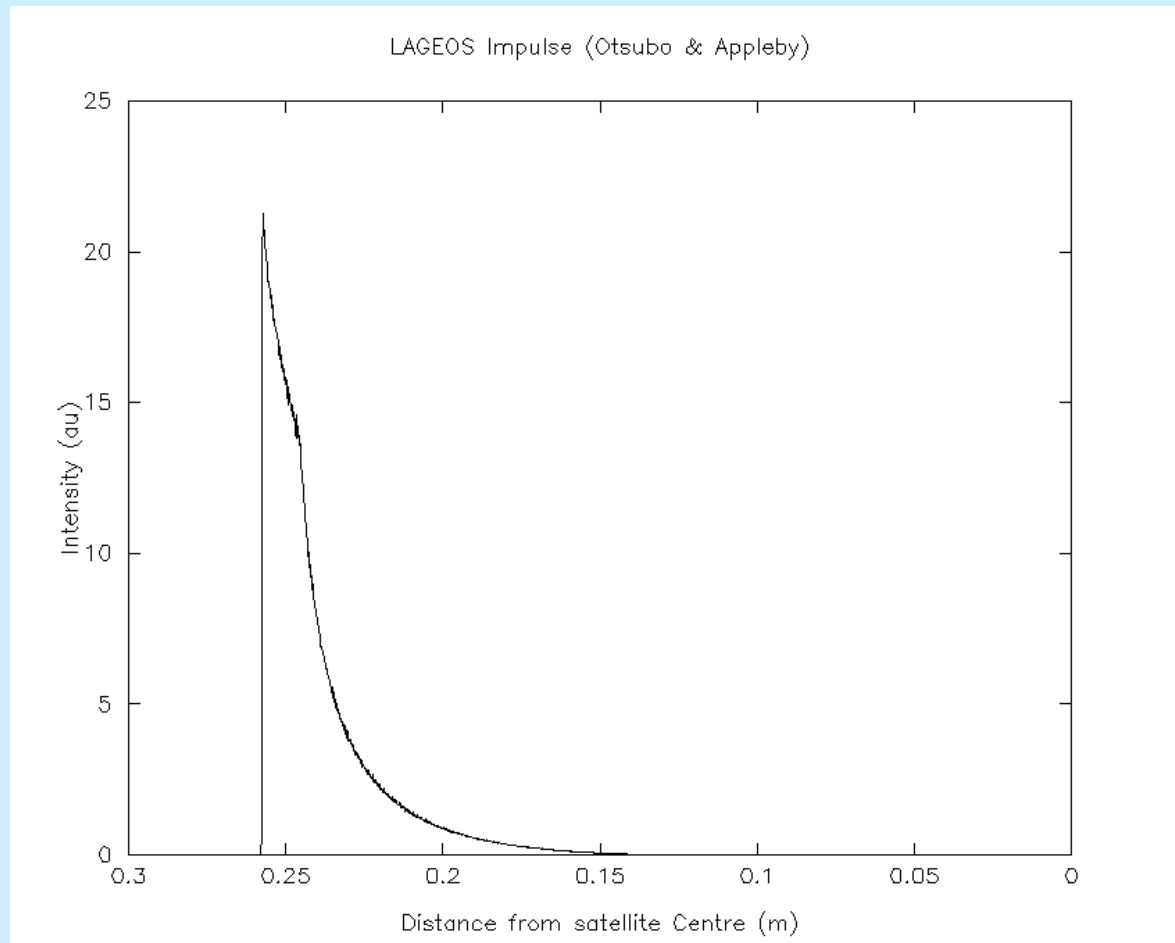
- Depending upon the stations' technology:
 - there is a range of appropriate CoM values;
 - for LAGEOS the total range is ~6mm (Minott *et al*, 1993, Otsubo & Appleby, 2003)
- Station technology:
 - multi-photon returns:
 - photomultiplier or first-photon detection
 - single photon return
- Development of a model, illustrated using a low return-energy system (single photons):

At single-photon, expect distribution of range residuals
to be convolution of whole-system response with
LAGEOS impulse

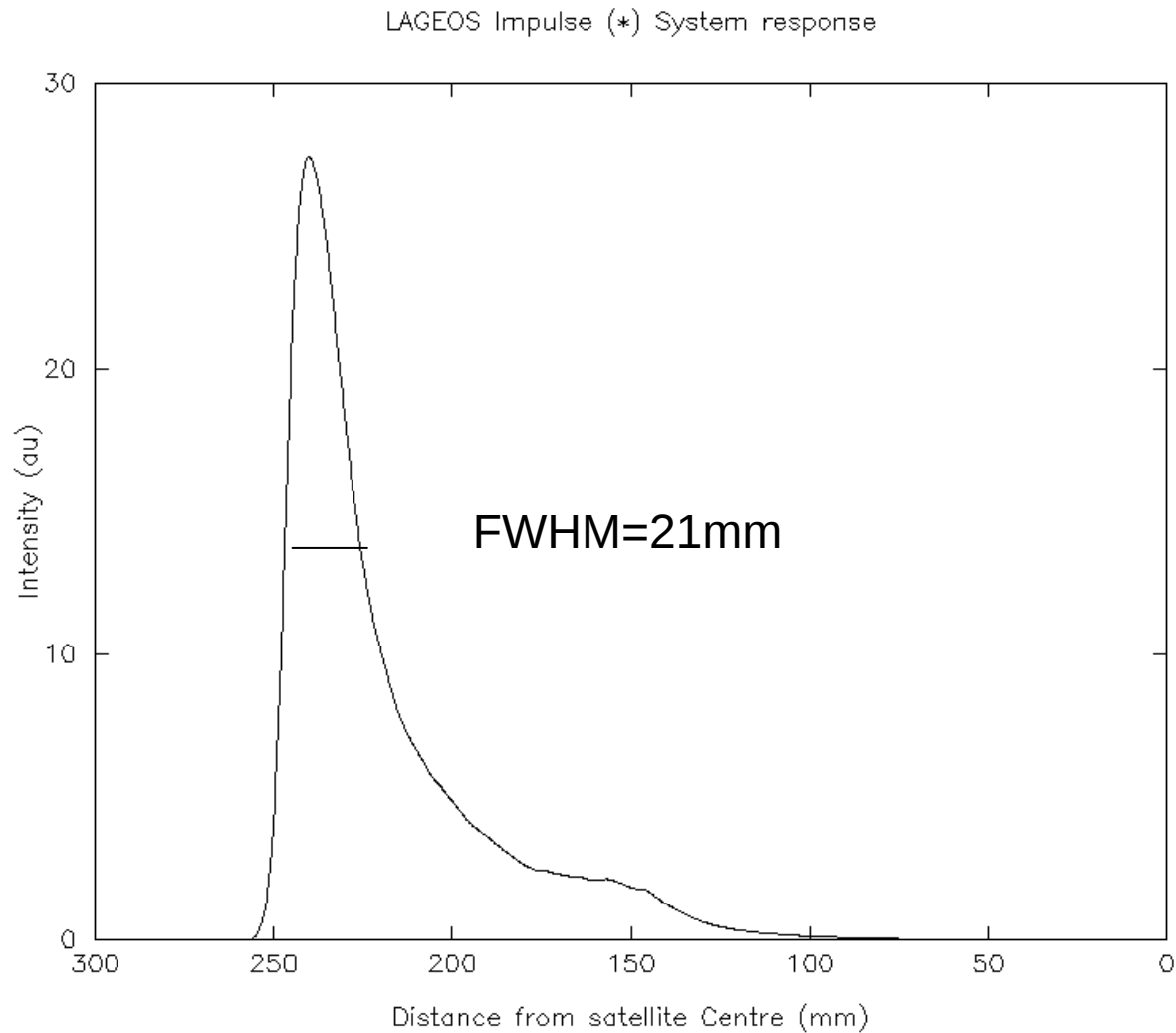


System response obtained from target-board ranging at $\ll$ single photons

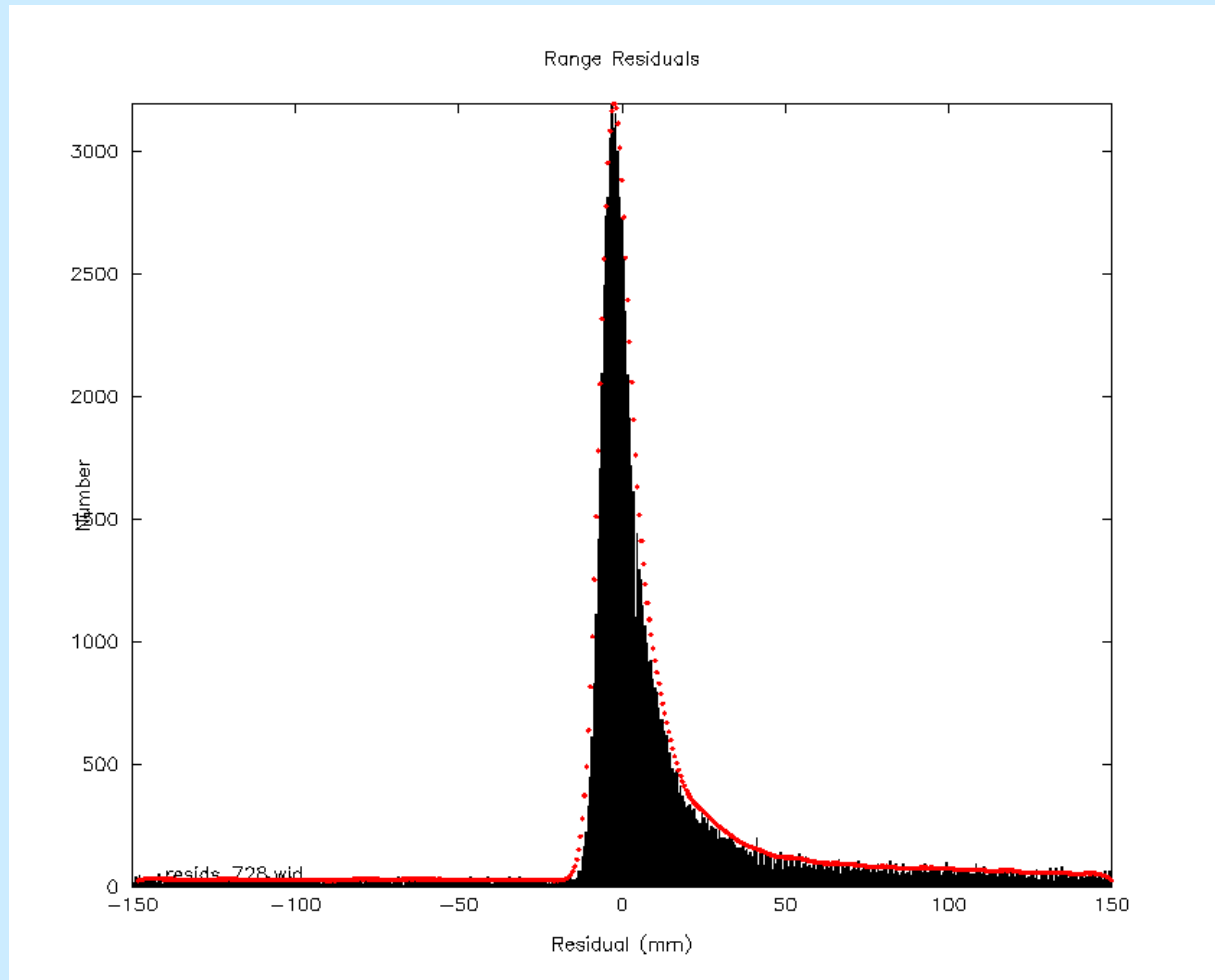
LAGEOS impulse (Otsubo & Appleby, 2003)



System (*) LAGEOS



Real data from a pass at $\ll$ single photons.
 $\sigma = 8.5\text{mm}$: (data will be rejected at -12 and $+25\text{mm}$)

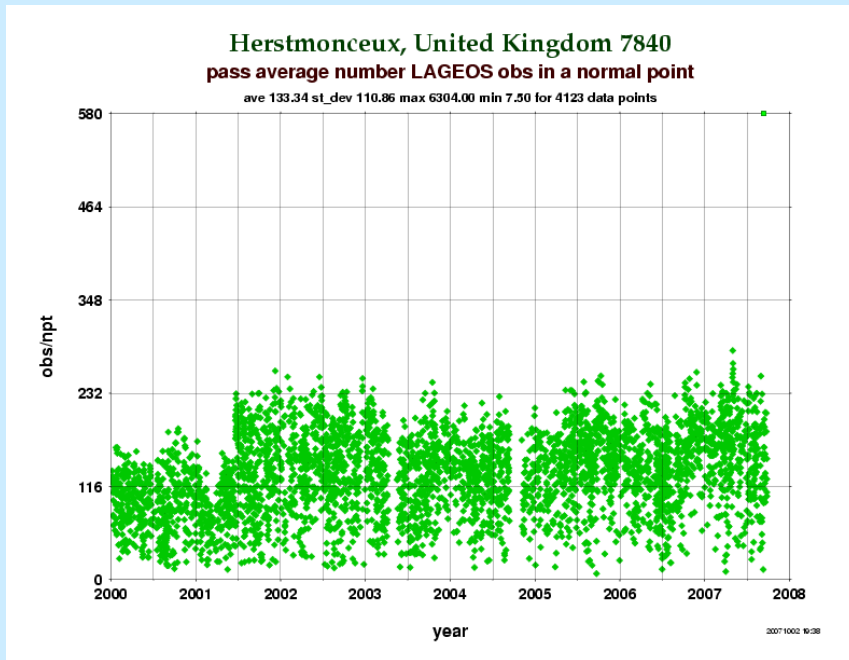


For this case, possible to compute **from the model** an **average CoM** value accurate to $\sim 1\text{mm}$ ($=245\text{mm}$)

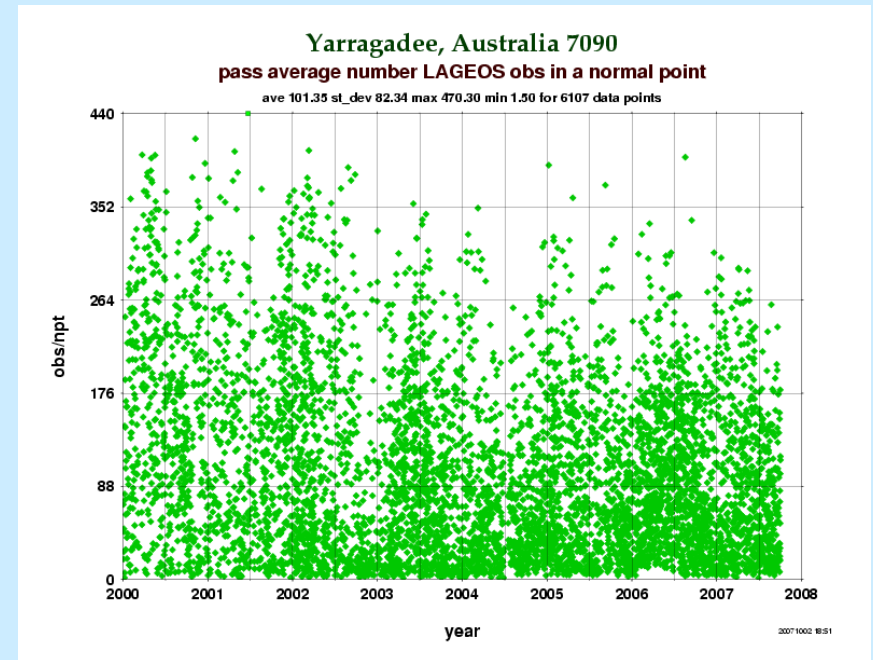
Centre of mass corrections >> single photons

- For NASA systems, for example, returns peak at several hundreds of photons (est. from link models, e.g. Degnan, 1993)
- Models for CoM depend upon characteristics of electronic discriminators;
- Cannot use statistical method for CoM as for single-photon systems
 - But can **estimate** from the model distributions (leading edge), to give CoM 248 ± 2 mm
 - This compares with ground tests on LAGEOS-2 giving 249 mm (Minott, 1993)

Single-photon vs multi-photon yield



Single-photon, consistent



Multi-photon, variable

In summary:

There exist different CoM values dependent on the stations' technology.

- Single photon systems have smallest uncertainty: **$\pm 1\text{mm}$**
- Com for high-energy systems have an estimated uncertainty of $\pm 2\text{mm}$
 - take account of unknown effect of discriminators at different stations;
 - effect is to increase effective pulse-length
- A table of values will be produced:
- CoM for typical single photon station 245mm
- Com for typical, majority, high-energy station 248mm
- Relative to 'standard' 251mm, change of $\sim 0.3\text{ppb}$.

Conclusion

- With improved
 - estimates of counters' effects in the sub-network;
 - knowledge of band of appropriate CoM values throughout the network:
 - LAGEOS is not a mm-level target for >single photons
- Should include these effects in future re-analyses efforts towards:
 - TRF;
 - GM: a change of CoM from 251 to 248 is 0.5ppb
 - Constrained RB for stations based on informed CoM band and counter characteristics.
- **NB** New technology (event timer, kHz) systems fulfil 'best practice' requirements.