

Experiences with CONT02 and GGOS-D,

Standardization / Extension of Common Parameters

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GGOS-D Parameters

Technique	Crd.	Pol.	UT/ LOD	Nut.	Cnm/ Snm	Geo- cent.	Trp. ZD	Trp. Grd.	Range Bias	Radio Sour.
VLBI (DGFI)	X	X	X	X			X	X		X
VLBI (IGGB)	X	X	X	X			X	X		X
GPS (Bernese)	X	X	X	X		X	X	X		
GPS (EPOS)										
SLR (DGFI)	X	X	X		X	(X)			X	
SLR (GFZ)	X	X	X		X	(X)			X	
LEO	X				X					
Altimetry	(X)				(X)	(X)				

GGOS-D Common Standards

Same state-of-the-art modeling, same parameterization for all techniques:

- **Station coordinates:** Solid Earth tides (IERS2003), pole tides (IERS2003), ocean tides (FES2004), ocean loading (FES2004)
 - **Earth rotation:** linear interpolation scheme, subdaily ERP model (IERS2003), nutation (IAU2000A)
 - **Troposphere (microwave):** hydrostatic delay (ECMWF grids), hydrostatic mapping (VMF1), wet delay and gradients estimated (piece-wise linear)
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- **Troposphere (optical):** Mendes and Pavlis (2004)
 - **GPS technique-specific:** phase center model (igs05_1421.atx), antenna heights and horizontal offsets (igs.snx), 2nd and 3rd order ionosphere
 - **VLBI technique-specific:** thermal deformation (Nothnagel, Skurikhina), reference temperature
 - **SLR technique-specific:** reflector offsets (ILRS), range biases (ILRS), arc-length 7 days

What do we need to combine?

Must represent same physical phenomenon:

- Time period
- A priori correction model
- Estimation model (parameterization)
- "Information free of deforming constraints" (direct / indirect)

Representation of linear functions

Options:

- **Mathematical representation**
 - one offset (e.g. at mean epoch) + one rate for each interval
 - functional values at interval borders, which are implicitly connected with a line
 - “others” (like in OCCAM)
- **Continuity at interval borders**
 - **Yes**
 - + reduces number of estimated parameters
 - + higher numerical stability
 - + “removes” jumps, which might not have physical meaning
 - **NO**
 - + to remove continuity can be difficult
 - + continuity might also not have physical meaning

A priori function n.e. parameterization

For comparisons & to combine, use

- * transformation to different epochs
- * transformation to different a priori values

= > Necessary (e.g. for EOP or ZD) :

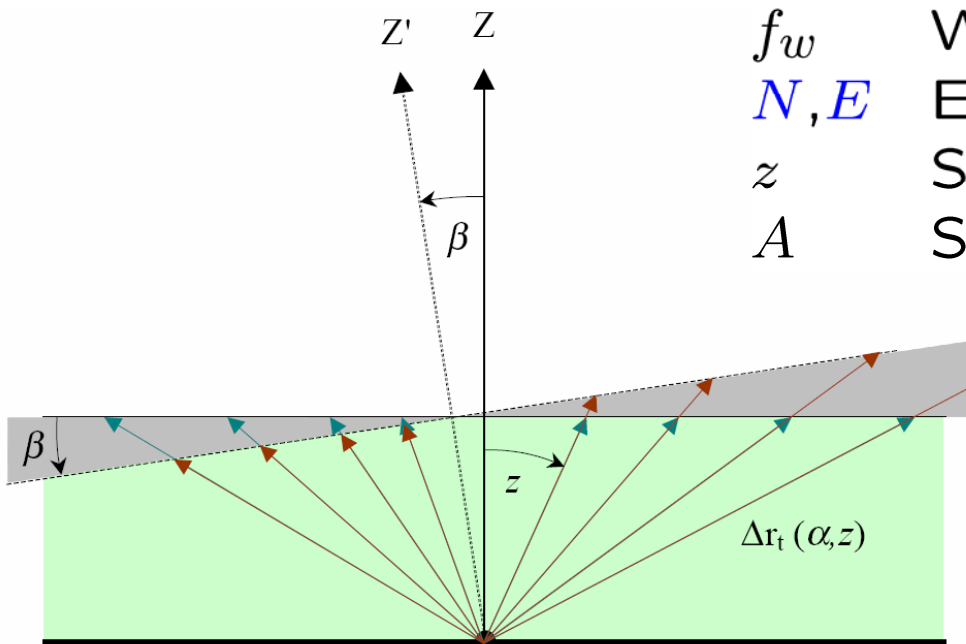
- * either: a priori function = estimated function
- * or: interpolation scheme must be fully given
(e.g. all polynomials of cubic spline)

Otherwise, the neglected terms will induce errors

Different types of gradient models

MacMillan (1995) $\text{GRD} = f_w(z) \tan z [N \cos A + E \sin A]$

Tilting model $\text{GRD} = \frac{\partial f_w}{\partial z} [N \cos A + E \sin A]$



f_w Wet mapping function
 N, E Estimated gradients
 z Satellite/quasar zenith angle
 A Satellite/quasar azimuth

Impact on:

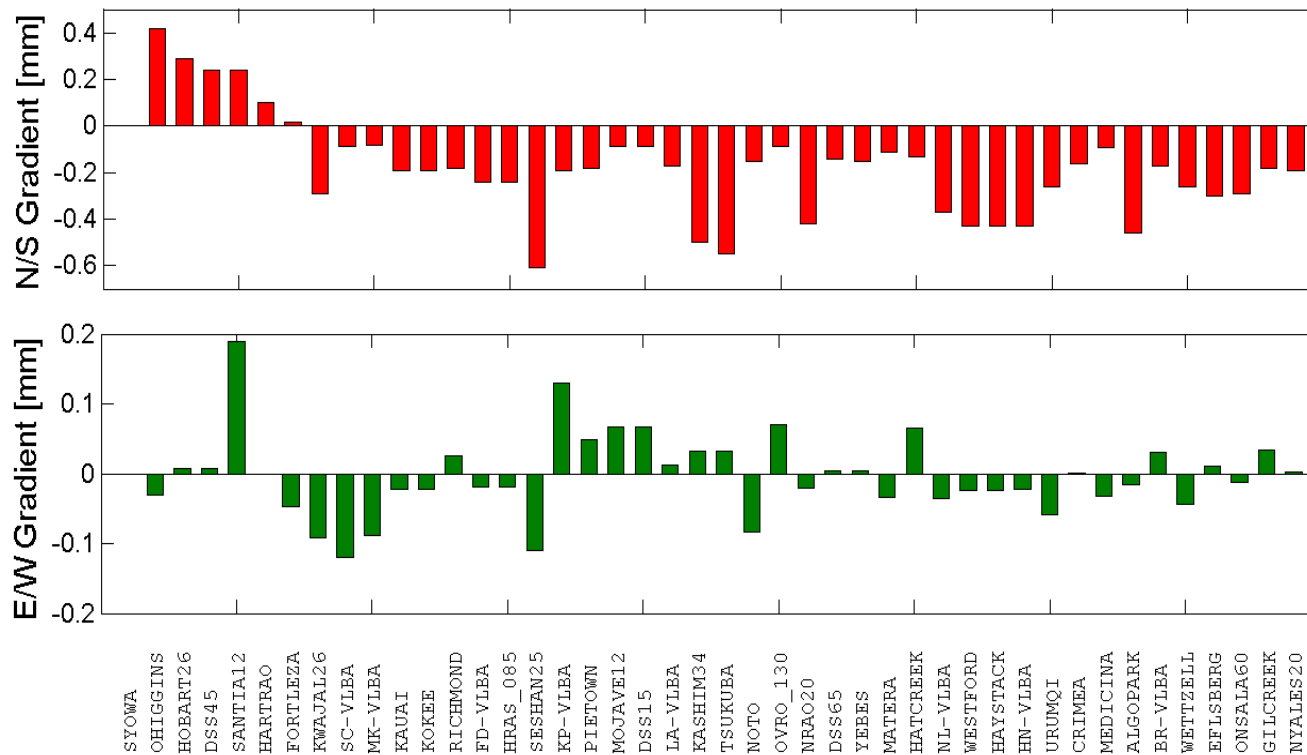
- Gradients: < 0.05 mm
- Coordinates: **up to 0.5 mm**

Tilting of the tropospheric zenith by the angle β .

Handling of a priori gradients

Is important, because:

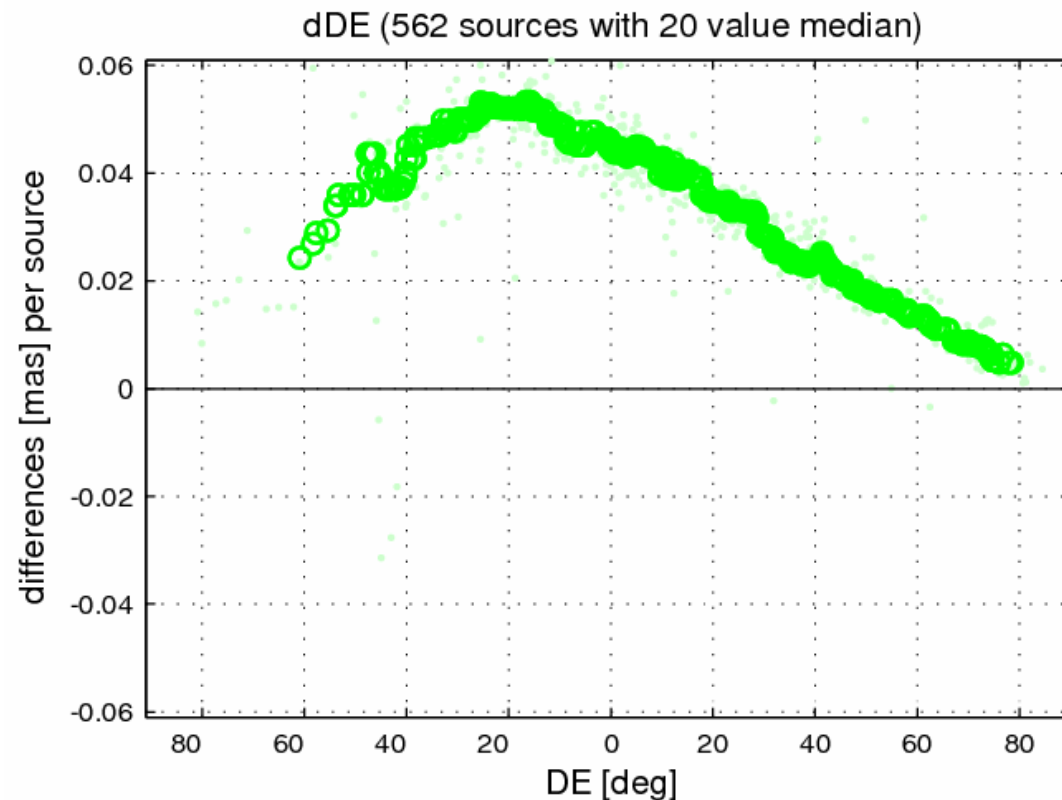
They are constrained in VLBI solutions (especially for old sessions)
=> directly affect reference frames (especially CRF)



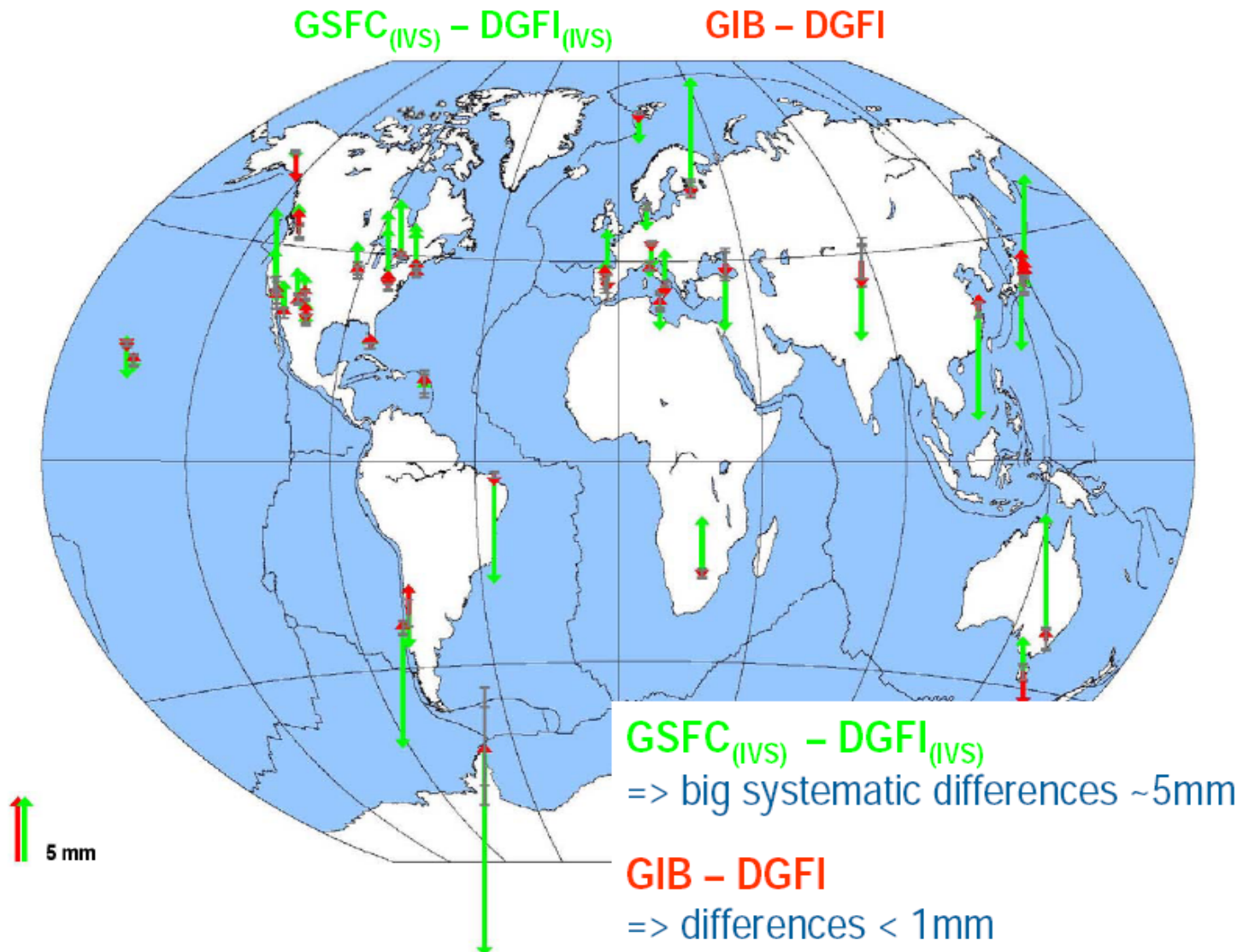
GSFC
DAO 90-95

Effect of a priori gradients (VLBI)

Source coordinates

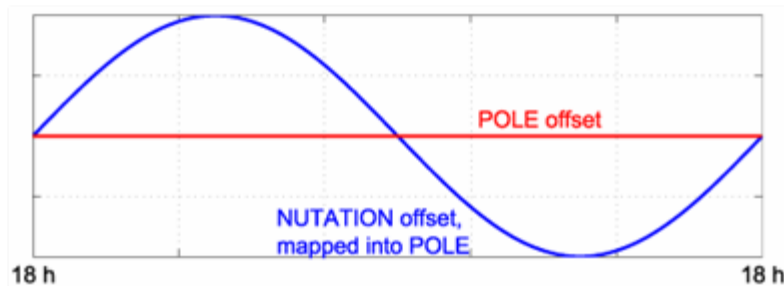


Pole tide model & effect on geodetic parameters

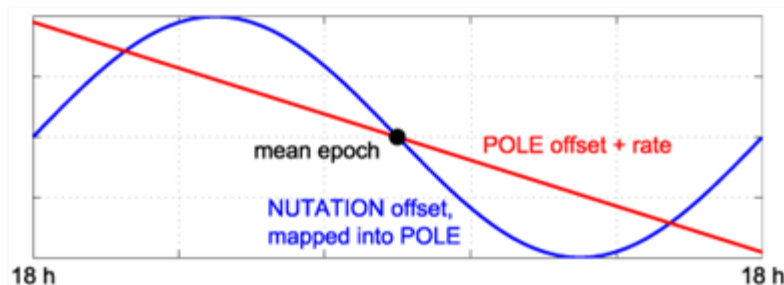


Polar motion and nutation and rates...

24 h, nutation offset, terrestrial pole offset and rate (terr. pole offset only vs. terr. pole offset and rate)



$$\text{Corr (nut. offset / terr. offset)} = 0$$



$$\begin{aligned}\text{Corr (terr. offset / terr. rate)} &= 0 \\ \text{Corr (nut. offset / terr. rate)} &\text{ NOT } 0 \\ \text{Corr (nut. offset / terr. offset)} &= 0\end{aligned}$$

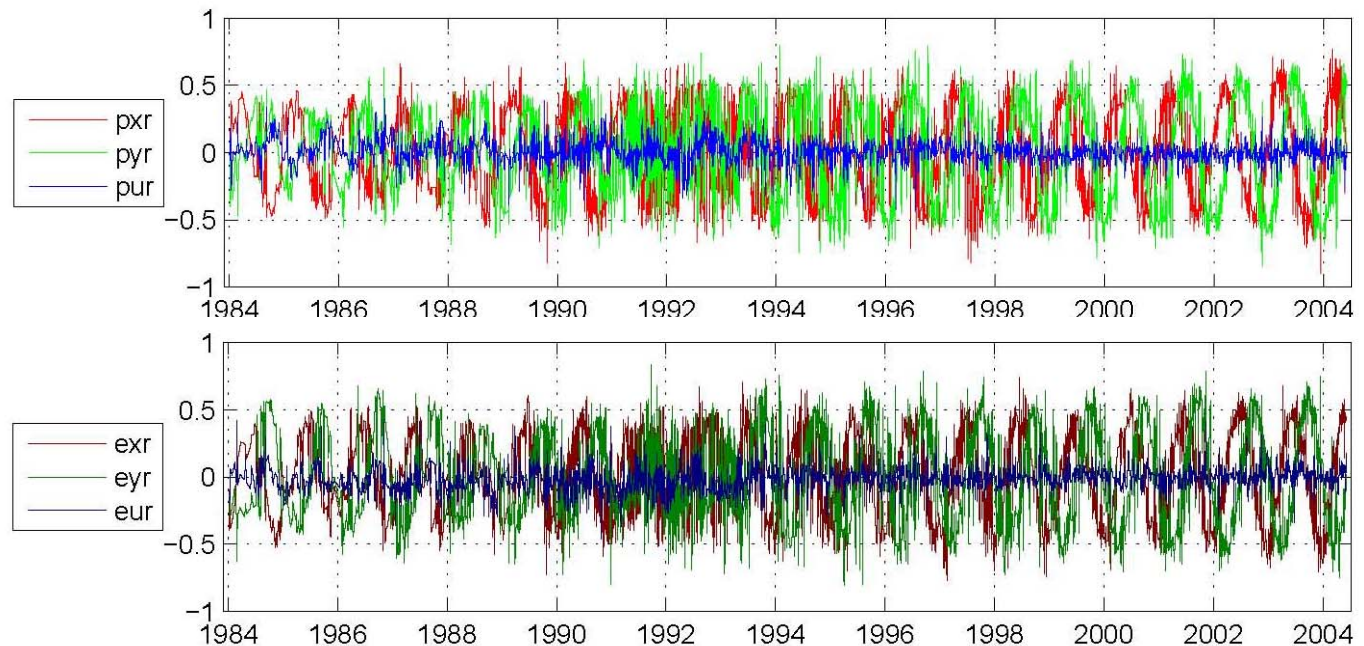
Polar motion and nutation and rates...

Estimated for 20 years VLBI-data:

terrestrial **offsets** + **rates**
celestial **offsets**

correlations

between terr. rates
& cel. offsets



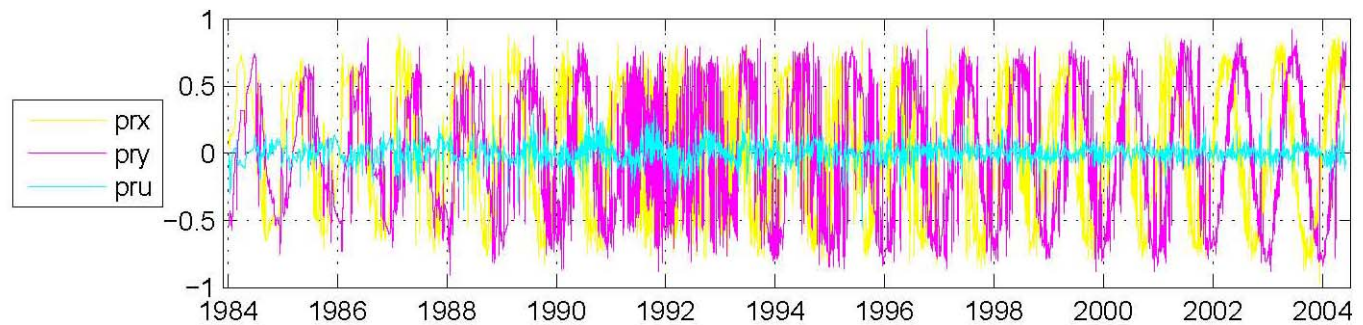
Polar motion and nutation and rates...

Estimated for 20 years VLBI-data:

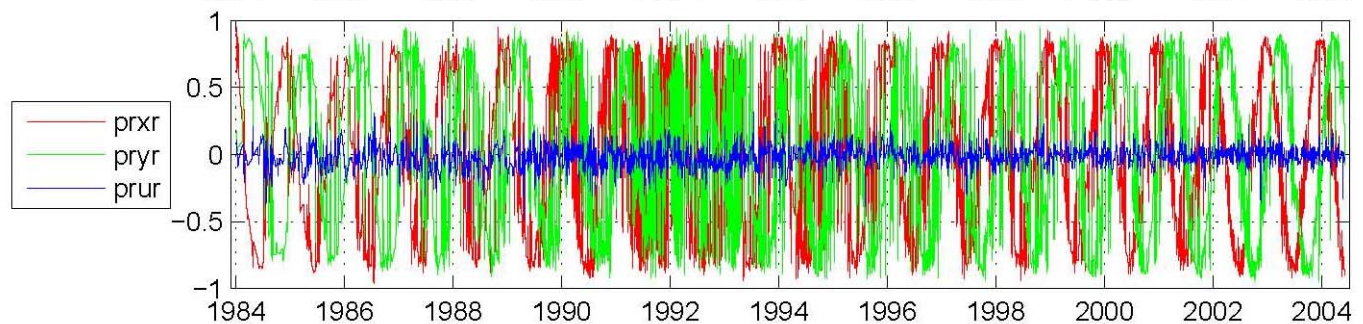
terrestrial **offsets** + **rates**

celestial **offsets** + **rates**

correlations
between terr. offset
& cel. rates



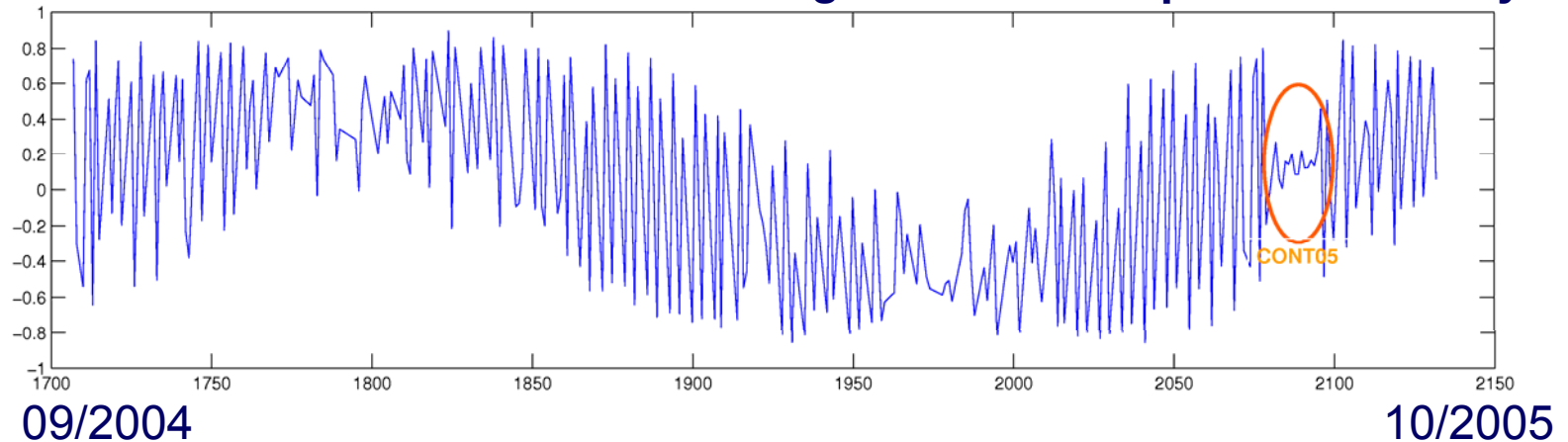
correlations
between terr. rates
& cel. rates



Polar motion and nutation and rates...

VLBI: Correlation between Nutation and Pole (parameterized as session polygon)

Correlation between Nutation in longitude and x pole for one year



Continuity during CONT05 campaign -> reduces correlation

Sub-daily polar motion and nutation

1) One-to-one correlation between nutation offset and retrograde diurnal PM:

$$x_p(t) = -\Delta \psi(t) \cdot \sin \varepsilon_0 \cdot \cos \theta - \Delta \varepsilon(t) \cdot \sin \theta$$

$$y_p(t) = -\Delta \psi(t) \cdot \sin \varepsilon_0 \cdot \sin \theta + \Delta \varepsilon(t) \cdot \cos \theta$$

=> Amplitude of retrograde diurnal PM: **CONSTANT**

$$C_{xy} = \sqrt{\Delta \varepsilon^2 + \Delta \psi^2 \cdot \sin^2 \varepsilon_0}$$

2) One-to-one correlation between nutation rate and retrograde diurnal PM:

$$x_p(\Delta t) = -\Delta \dot{\psi} \cdot \sin \varepsilon_0 \cdot \Delta t \cdot \cos \theta - \Delta \dot{\varepsilon} \cdot \Delta t \cdot \sin \theta$$

$$y_p(\Delta t) = -\Delta \dot{\psi} \cdot \sin \varepsilon_0 \cdot \Delta t \cdot \sin \theta + \Delta \dot{\varepsilon} \cdot \Delta t \cdot \cos \theta$$

=> Amplitude of retrograde diurnal PM: **TIME VARIABLE**

$$C_{xy}(\Delta t) = \Delta t \cdot \sqrt{\Delta \dot{\varepsilon}^2 + \Delta \dot{\psi}^2 \cdot \sin^2 \varepsilon_0}$$

Improved models => “improved” results ?

- * **fully reprocessed** GPS (Bernese5.1) and VLBI data (OCCAM6.1)

- * a priori models **homogenized**

=> GPS and VLBI height time series 94-07

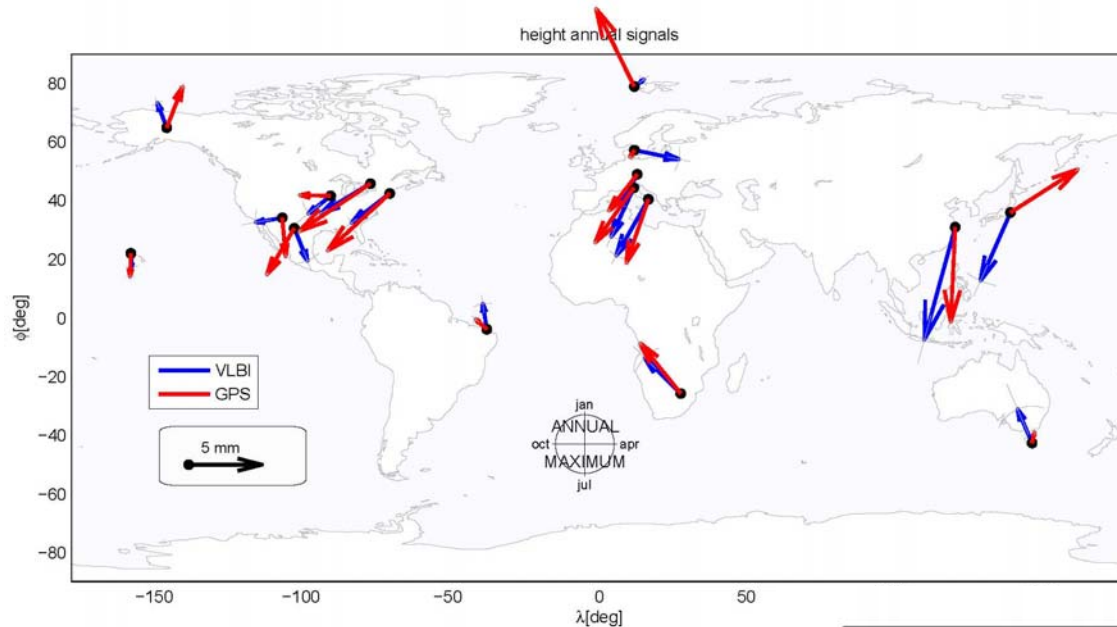
Iteration 1: “old” a priori models (NMF, constant a priori ZD ...)

Iteration 2: state of the art a priori models (VMF1, ZD from ECMWF ...)

=> TEST 1: similarity of GPS & VLBI annual signals

TEST 2: similarity of estimated atmo.-loading coefficients

Similarity of annual signals

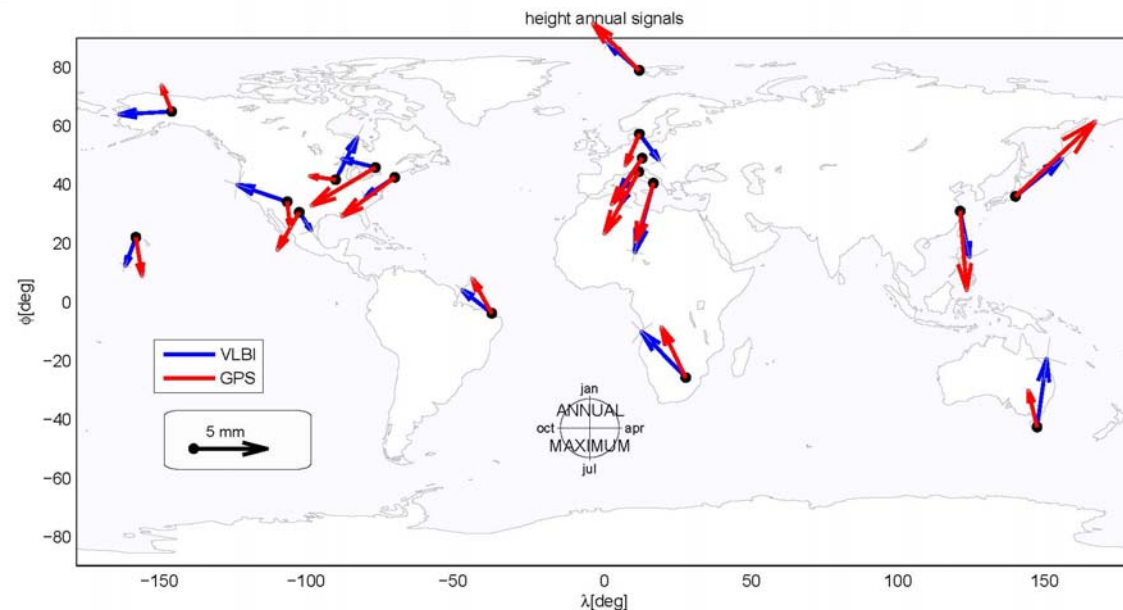


Iteration 1: “old” a priori models (NMF, constant a priori ZD ...)

WRMS GPS/VLBI:
2.2 mm amplitude
44 deg phase

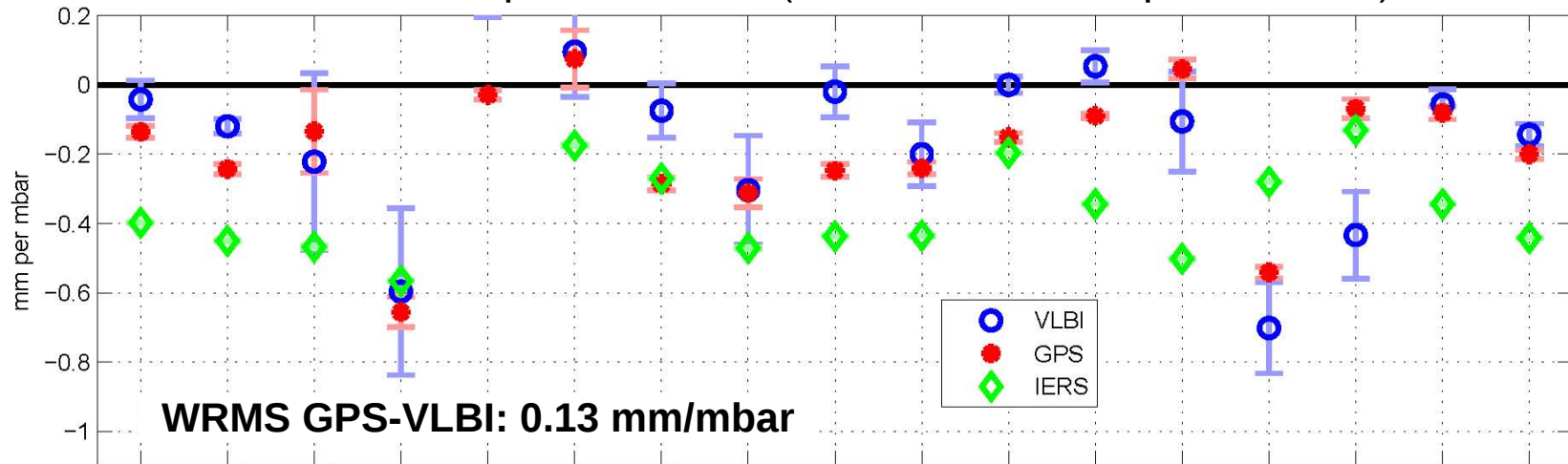
Iteration 2: state of the art a priori models (VMF1, ZD from ECMWF ...)

WRMS GPS/VLBI:
1.7 mm amplitude
38 deg phase



Similarity of estimated atmo-load coefficients

Iteration 1: “old” a priori models (NMF, constant a priori ZD ...)



Iteration 2: state of the art a priori models (VMF1, ZD from ECMWF ...)

